

K2-140b – an eccentric 6.57 d transiting hot Jupiter in Virgo

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ABSTRACT

We present the discovery of K2-140b, a $P = 6.57$ d Jupiter-mass ($M_P = 1.019 \pm 0.070 M_{\text{Jup}}$) planet transiting a $V = 12.5$ (G5-spectral type) star in an eccentric orbit ($e = 0.120^{+0.056}_{-0.046}$) detected using a combination of K2 photometry and ground-based observations. With a radius of $1.095 \pm 0.018 R_{\text{Jup}}$, the planet has a bulk density of $0.726 \pm 0.062 \rho_{\text{Jup}}$. The host star has a $[\text{Fe}/\text{H}]$ of 0.12 ± 0.045 , and from the K2 light curve, we find a rotation period for the star of 16.3 ± 0.1 d. This discovery is the 9th hot Jupiter from K2 and highlights K2’s ability to detect transiting giant planets at periods slightly longer than traditional, ground-based surveys. This planet is slightly inflated, but much less than others with similar incident fluxes. These are of interest for investigating the inflation mechanism of hot Jupiters.

Key words: techniques: high angular resolution – techniques: photometric – techniques: radial velocities – planets and satellites: detection – stars: individual: K2-140.

1 INTRODUCTION

Transiting exoplanets offer the best insight into worlds outside our Solar system, as we can determine the mass, radius, and obtain information regarding the planetary atmosphere. Traditional ground-based surveys such as HAT-Net (Bakos et al. 2004), WASP (Pollacco et al. 2006) and KELT (Pepper et al. 2007) are predominately sensitive to very short period transiting giant planets ($P \sim 3$ d). Longer

period transiting systems have proved much more difficult to detect. Some advantage has been gained using multisite surveys, with HAT-South (Bakos et al. 2013) detecting planets in periods as long as 16 d (Brahm et al. 2016b). However, the continuous monitoring enabled by space-based telescopes has allowed for a dramatic increase in the number of longer period transiting systems. The *Kepler* mission (Borucki et al. 2010; Jenkins et al. 2010; Koch et al. 2010), with 4 yr of near-continuous coverage, has uncovered a host of transiting planets with longer periods, however many of these transit stars that are too faint to allow for planetary mass determination via radial velocities. In 2013, after 4 yr of observations, the second of *Kepler*’s

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four reaction wheels failed. From this, the *K2* mission was born (Howell et al. 2014). Unlike the original mission, which observed a single region of the sky, *K2* observes proposed targets within a series of fields lying along the ecliptic, continuously, for ~ 80 d. The adverse impact of the two failed reaction wheels has been minimized, but there is now a 6-h roll effect affecting *K2* light curves. This causes brightness changes as stars move from pixel to pixel on the CCD. However, there have been many different attempts to calibrate this effect and remove it from the light curves, allowing for transiting exoplanet searches (Vanderburg & Johnson 2014; Armstrong et al. 2015; Aigrain, Parviainen & Pope 2016). Further, the continuous observations for 80 d still allows for longer period systems to be discovered, e.g. EPIC 201702477b (40.736d, Bayliss et al. 2017b). Additionally, a number of more typical hot Jupiters have been discovered, e.g. K2-30b (4.099d), K2-34b (2.996d) (Lillo-Box et al. 2016), and K2-31b (1.258d, Grziwa et al. 2016).

In this paper, we report the discovery of K2-140b, a 6.57-d hot Jupiter on an eccentric orbit. In Section 2, we outline the observations that led to the discovery. In Section 3, we describe the analysis of the data that determined its properties. In Section 4, we discuss the properties and the planet’s position with respect to other known hot Jupiters, and in Section 5, we summarize the discovery.

2 OBSERVATIONS

In this section, we set out the observations made to detect and characterize the transiting exoplanet K2-140b.

2.1 *K2* Photometry

The light curve for K2-140 came from Campaign 10 of the *K2* mission. This campaign observed 41 607 targets in long cadence (30 min) and 138 targets in short cadence (1 min) in the ecliptic plane centred around RA 12h 27m 07.07s Dec. $-04^{\circ} 01' 37.77''$. Due to a pointing error (targets were off by 12 arcsec, meaning many fell outside their apertures), this campaign was split into two data releases, C10a and C10b. C10a lasted 6 d between 2016 July 6 19:45:29 UTC and 2016 July 13 01:19:55 UTC. The second release, C10b, was observed for 69 d. However, there was a data gap of 14 d after 7 d of observing due to module 4 of the telescope failing which powered off the photometer.

After the public release of the data on 2016 December 20, the light curves reduced by the *K2* Science team were downloaded and analysed for planetary signals (light-curve data listed in Table 2). This analysis required long-term variations to be removed from the light curve. This was done by fitting a sliding polynomial, which fits locally a polynomial to a small section (‘step size’) of the light curve using a significantly larger section (‘window’) of the surrounding light curve, and dividing it out. For the sliding polynomial, we used a third-order polynomial with a step size of 0.1 d and a window size of 5 d. To ensure the result is not jagged, the step size must be significantly smaller than the window size and to ensure that the transit is not accidentally fitted and removed by the process, to ensure the transit is left intact requires outlier rejection from the polynomial fit – this was done with a strict cut of positive outliers and a looser negative outlier cut. To search for planetary transits, we used a PYTHON-wrapped¹ version of the BLS routine (Kovács, Zucker & Mazeh 2002) to initially search for any significant signals and then a second time focused on the signal of interest to determine

the transit parameters as accurately as possible. We then phase fold and output the light curve for visual inspection. This transit search found many candidates, which included K2-140 – a 6.57-d planet with a 1.26 per cent transit signal (Fig. 1).

Additionally, as can be seen in Fig. 1, there is some evidence of aliasing in the cadence. This is due to the observed rotation period being a half integer multiple of the cadence of *K2*.

2.2 Radial velocities

We observed K2-140 using the CORALIE spectrograph (Queloz et al. 2000) on the 1.2-m Euler Telescope at La Silla Observatory in Chile. CORALIE is a fibre-fed, high resolution ($R = 60\,000$) echelle spectrograph capable of delivering $<6\text{ m s}^{-1}$ accuracy. Observations were made between 2017 February 20 and 2017 April 8. Additionally, K2-140 was observed using the High Accuracy Radial Velocity Planet Searcher (HARPS, Mayor et al. 2003) mounted on the ESO 3.6-m telescope in La Silla Observatory in Chile, on February 22 and between April 23 and 28. The spectra, which have a resolution $R = 115\,000$, were reduced using the Collection of Elemental Routines for Echelle Spectra (CERES, Brahm, Jordán & Espinoza 2017a).

The associated errors with each instrument vary significantly. In the case of CORALIE, the initial errors are higher than HARPS primarily because the star is relatively faint. As a test for the errors, we also calculated the root-mean-square of the data points from the fitted model (see Section 3.2) and they were comparable to the measured errors (see Table 1).

The radial velocities are plotted in Fig. 2, along with the best-fitting model determined by the joint fit described in Section 3.2. The radial velocities are also presented in Table 3.

In order to check radial velocity variation induced by a blended spectrum, we computed the bisector slope of the cross-correlation function for each observation in the manner described in Queloz et al. (2001). In Fig. 3, we find no correlation between the bisector slope and the measured radial velocity. If the signal detected was due to a blended eclipsing binary, then we may expect to see a strong correlation between the bisectors and radial velocity measurements. The bisector values are presented with the radial velocities in Table 3.

2.3 LCO photometry

In order to refine the ephemeris, check for TTVs, and check for a colour-dependent transit depth (signifying a probable blend), we performed ground-based photometric follow-up using the Las Cumbres Observatory (LCO) 1-m telescope network (Brown et al. 2013). On 2017 March 18, we monitored the transit in the *i*-band using the three LCO 1-m telescopes situated at South Africa Astronomical Observatory at Sutherland, South Africa (Fig. 4). The observations were taken using the ‘Sinistro’ camera with exposure times of 120 s and the telescope defocused (2.0 mm) to avoid saturation and spread the stellar point-spread function over more pixels – reducing the impact of flat-fielding uncertainties. The images were reduced using the standard LCO reduction pipeline (BANZAI), and then aperture photometry was performed using an automated pipeline (Espinoza et al., in preparation). These observations were made as part of a wider LCO Key Project² to characterize transiting planets using the

¹ <https://github.com/dfm/python-bls>

² <http://web.gps.caltech.edu/shporer/LCOKP/>

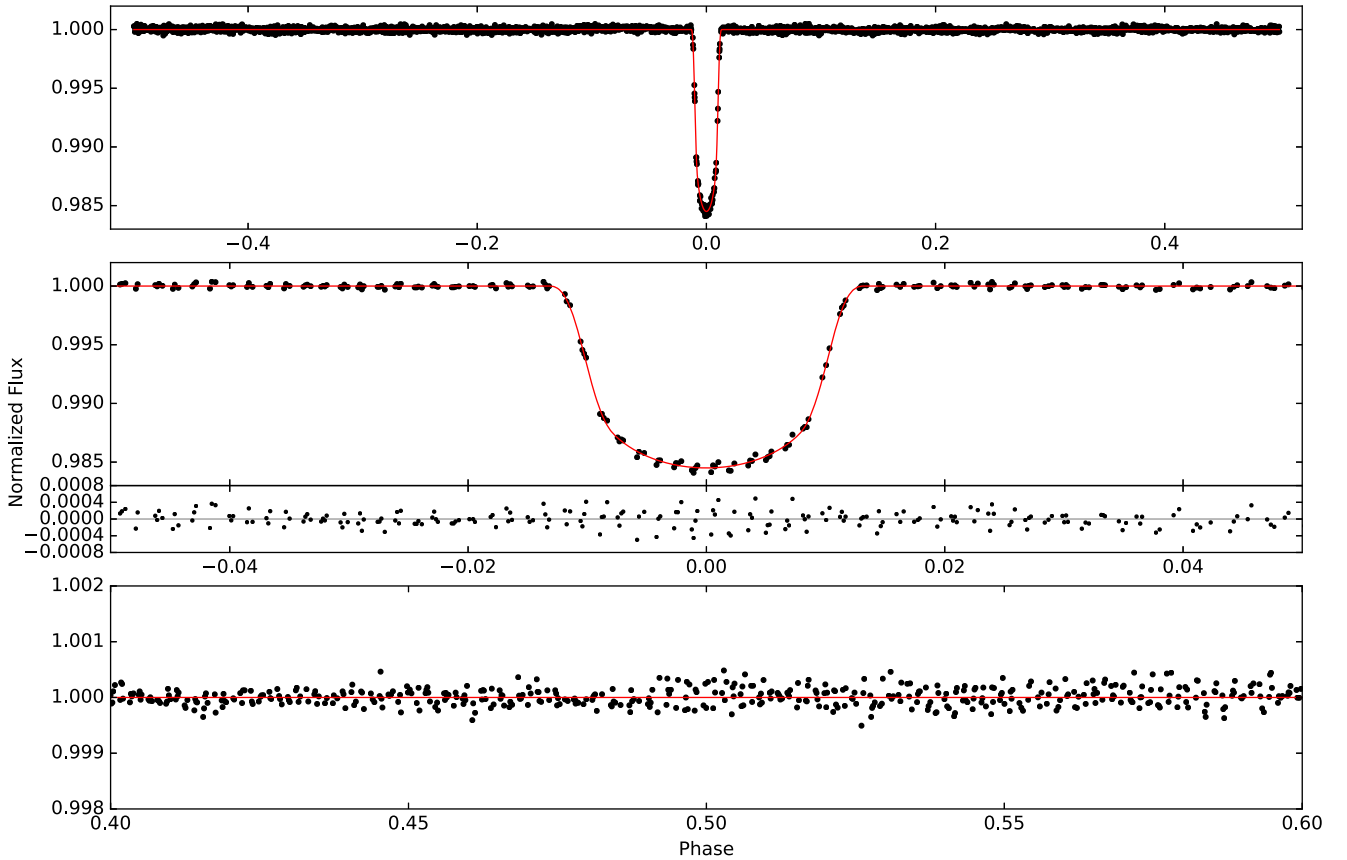


Figure 1. Phase-folded *K2* light curve of K2-140 (black points) with best-fitting model plotted as a solid red line (see Section 3.2). Top panel: Full phase light curve with the transit of K2-140b. There are no other significant dips indicating any other transits. Middle panel: Zoom-in of the transit of K2-140b and the resulting residuals from it and the model fit. Bottom panel: Zoom-in around phase 0.5. There is no indication of an observable secondary eclipse.

LCO 1-m network (see Bayliss et al. 2017b). They are listed in Table 2.

2.4 High angular resolution imaging

High angular resolution imaging of the target was obtained using the Robo-AO instrument (Baranec et al. 2013, 2014) mounted on the Kitt Peak 2.1-m telescope, on the night of 2017 April 15 using the long-pass ‘*lp600*’ filter (Baranec et al. 2014) with a seeing of 1.5 arcsec and Strehl ratio of 2.7 per cent. The raw rapid read-out data from the Robo-AO visual camera were processed using Robo-AO’s reduction pipelines described briefly below. A more detailed description can be found in Jensen-Clem et al. (2017).

First, the ‘bright-star pipeline’ generates a windowed data cube centred on an automatically selected guide star. The windowed region is bi-cubically up-sampled and cross correlated with the theoretical PSF to give the centre coordinates of the guide star’s PSF in each frame. The nightly dark and dome flat exposures are then used to calibrate the full-frame, unprocessed images. The calibrated full frames are aligned using the centre coordinates identified by the up-sampled, windowed frames, and co-added via the Drizzle algorithm.

Next, the ‘high contrast imaging pipeline’ generates a 3.5 arcsec frame windowed about the star of interest in the final science frame from the bright star pipeline. A high pass filter is applied to the windowed frame to reduce the contribution of the stellar halo. To whiten correlated speckle noise at small angular separations from

the target star, a synthetic PSF generated by the Karhunen–Loève Image Processing (KLIP) algorithm is subtracted from the frame. The KLIP algorithm is based on the method of principal component analysis. The PSF diversity needed to create this synthetic image is provided by a reference library of Robo-AO observations – a technique called Reference star Differential Imaging.

The contrast curve was estimated using the VIP (Vortex Image Processing) package (Gomez Gonzalez et al. 2016) by measuring the residuals from resolution element-sized regions in the PSF-subtracted image.

The final Robo-AO image and contrast curve are shown in Fig. 5. The target is isolated down to $\Delta\text{mag} = 4$ at 0.5 arcsec and $\Delta\text{mag} = 4.5$ at 1 arcsec.

3 ANALYSIS

3.1 Stellar parameters

Initially, to determine the stellar parameters of K2-140, we built a pipeline for CORALIE spectra based on *ISPEC*³ (Blanco-Cuaresma et al. 2014). This tool provides a large number of options to treat high-resolution spectra (e.g. co-addition, continuum normalization) and it can derive atmospheric parameters and chemical abundances using many different model atmospheres, atomic line lists,

³ <http://www.blancocuaresma.com/siSpec>

Table 1. Parameters of K2-140.

Parameter	Units	Value	Source
EPIC ID		228735255	H16 ^a
2MASS ID		2MASS J12323296-0936274	H16 ^a
RA (α)	hh:mm:ss	12: 32: 32.96	H16 ^a
Dec. (δ)	dd:mm:ss	−09: 36: 27.5	H16 ^a
g _{GAIA}	mag	12.393	GAIA ^b
<i>B</i>	mag	13.349 ± 0.030	APASS ^c
<i>V</i>	mag	12.624 ± 0.030	APASS ^c
<i>g</i>	mag	12.930 ± 0.060	APASS ^c
<i>r</i>	mag	12.426 ± 0.020	APASS ^c
<i>i</i>	mag	12.292 ± 0.050	APASS ^c
<i>J</i>	mag	11.421 ± 0.026	APASS ^c
<i>H</i>	mag	11.068 ± 0.021	APASS ^c
<i>K_s</i>	mag	10.995 ± 0.021	2MASS ^d
<i>K_{ep}</i>	mag	12.483	H16 ^a
<i>W₁</i>	mag	10.985 ± 0.024	ALLWISE ^e
<i>W₂</i>	mag	11.030 ± 0.021	ALLWISE ^e
<i>W₃</i>	mag	10.891 ± 0.119	ALLWISE ^e
<i>W₄</i>	mag	8.898 ± −	ALLWISE ^e
Distance	pc	340.24 ± 11.58	<i>f</i>
Age	Gyr	4.22 ± 0.95	<i>f</i>
Spectral type		G5	<i>f</i>
<i>M_V</i>	mag	4.965 ^{+0.069} _{−0.066}	<i>f</i>
[Fe/H]	dex	0.12 ± 0.045	<i>f</i>
<i>T_{eff}</i>	K	5654 ± 55	<i>f</i>
log(<i>g</i>)	dex	4.452 ^{+0.010} _{−0.009}	<i>f</i>
<i>v sin i</i>	km s ^{−1}	3.8 ± 0.2	<i>f</i>
<i>P_{rot}</i>	days	16.3 ± 0.1	<i>f</i>
<i>M_*</i>	<i>M_⊙</i>	1.005 ^{+0.021} _{−0.020}	<i>f</i>
<i>R_*</i>	<i>R_⊙</i>	0.987 ^{+0.011} _{−0.011}	<i>f</i>
ρ_*	ρ_{\odot}	1.048 ± 0.041	<i>f</i>
<i>L_*</i>	<i>L_⊙</i>	0.893 ^{+0.049} _{−0.048}	<i>f</i>
$\mu_{1,K2}$		0.341 ^{+0.084} _{−0.079}	<i>f</i>
$\mu_{2,K2}$		0.441 ^{+0.111} _{−0.079}	<i>f</i>
$\mu_{1,LCO}$		0.56 ^{+0.18} _{−0.16}	<i>f</i>
$\mu_{2,LCO}$		0.38 ^{+0.20} _{−0.17}	<i>f</i>
RV residuals (CORALIE)	km s ^{−1}	0.0184	<i>f</i>
RV residuals (HARPS)	km s ^{−1}	0.0097	<i>f</i>

^aHuber et al. (2016), ^bGaia Collaboration et al. (2016a,b),^cHenden & Munari (2014), ^dSkrutskie et al. (2006),^eWright et al. (2010); Mainzer et al. (2011), ^fThis work

radiative transfer codes, and spectroscopic techniques (i.e. equivalent width and synthetic spectral fitting). For this study, we executed the following steps:

- (i) Align and co-add all the observations taken with CORALIE (see Section 2.2) to increase the S/N.
- (ii) Reduce the spectrum to the optical wavelength range (480–680 nm).
- (iii) Cross-correlate with a solar template to shift the observed spectrum to the rest frame.
- (iv) Discard negative fluxes and estimate flux errors based on an estimated S/N.
- (v) Convolve to a resolution of $R \sim 47\,000$ and homogeneously re-sample the spectrum.
- (vi) Ignore regions affected by telluric lines.
- (vii) Fit the pseudo-continuum and normalize the spectrum.
- (viii) Derive atmospheric parameters using the synthetic spectral fitting technique, SPECTRUM (Gray & Corbally 1994) as radiative

transfer code, atomic data obtained from VALD (Kupka, Dubernet & VAMDC Collaboration 2011), a line selection based on a $R \sim 47\,000$ solar spectrum (Blanco-Cuaresma et al. 2016, 2017) and the MARCS model atmospheres (Gustafsson et al. 2008).

As an output we obtained the effective temperature, surface gravity (log *g*), and metallicity. From these, a series of isochrones were generated using stellar model generator SYCLIST⁴ (Mowlavi et al. 2012). A grid of ages at a given metallicity ($Z = 0.040$) was generated and interpolated to determine the stellar age, mass, radius, and luminosity.

The results of the ISPEC analysis gave an effective temperature of 5732 ± 32 K, a log *g* of 4.29 dex and [Fe/H] = 0.32 ± 0.03 dex.

Following a similar procedure, the individual HARPS spectra were median combined in order to construct a higher SNR template.

⁴ <https://obswww.unige.ch/Recherche/evoldb/index/>

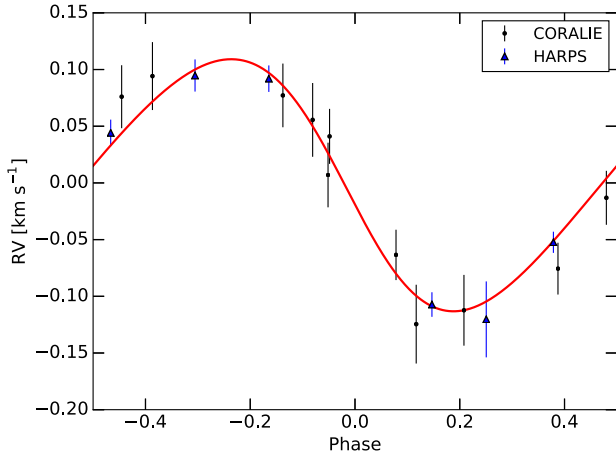


Figure 2. Phase-folded observations from CORALIE (black points) and HARPS (blue triangles) with the best-fitting model (red solid line) as described in Section 3.2. CORALIE observations were taken between 2017 February 20 and 2017 April 8 using the Swiss Euler telescope in La Silla, Chile. HARPS observations were taken between 2017 February 22 and 2017 April 28 using the ESO 3.6-m telescope in La Silla, Chile. The errors for HARPS have had the jitter added in quadrature.

Table 2. Photometry for K2-140.

BJD-2450000	Flux	Flux error	Filter	Instrument
7582.5906314203	1.000 020 94	0.000 083 99	kep	K2
7582.6110636177	1.000 065 07	0.000 083 93	kep	K2
7582.6314957142	1.000 003 89	0.000 083 85	kep	K2
7582.6519277110	1.000 017 66	0.000 083 76	kep	K2
7582.6723599071	1.000 004 62	0.000 083 69	kep	K2
7582.6927920026	0.999 985 20	0.000 083 62	kep	K2
7582.7132239980	1.000 019 08	0.000 083 51	kep	K2
7582.7336561931	0.999 929 69	0.000 083 42	kep	K2
7582.7540882872	1.000 152 49	0.000 083 31	kep	K2
7582.7745202812	0.999 933 07	0.000 083 23	kep	K2
–	–	–	–	–

*Note: partial list – full table available in electronic form.

Table 3. Radial velocities for K2-140b in chronological order.

BJD-2450000	RV km s ⁻¹	RV error km s ⁻¹	BIS	Instrument
7804.751722	1.25803	0.02389	–0.03886	CORALIE
7806.7167899	1.1231	0.0333	–0.019	HARPS
7814.792453	1.20384	0.02344	–0.08219	CORALIE
7815.668909	1.31119	0.02967	–0.03487	CORALIE
7817.678137	1.27255	0.03227	–0.06864	CORALIE
7818.723682	1.15348	0.02183	–0.01804	CORALIE
7820.754834	1.14137	0.02247	0.02071	CORALIE
7821.852054	1.29300	0.02745	0.03278	CORALIE
7823.874191	1.29414	0.02778	0.02189	CORALIE
7832.714263	1.10465	0.03093	–0.06040	CORALIE
7836.681188	1.31122	0.03383	0.00470	CORALIE
7850.717632	1.22394	0.02820	–0.05072	CORALIE
7851.823385	1.09243	0.03450	–0.00820	CORALIE
7866.6826602	1.1911	0.0086	0.02	HARPS
7867.699734	1.2876	0.0111	–0.009	HARPS
7868.7574426	1.3382	0.0137	0.003	HARPS
7869.6828912	1.3354	0.0111	0.039	HARPS
7871.7285204	1.1362	0.0102	0.0	HARPS

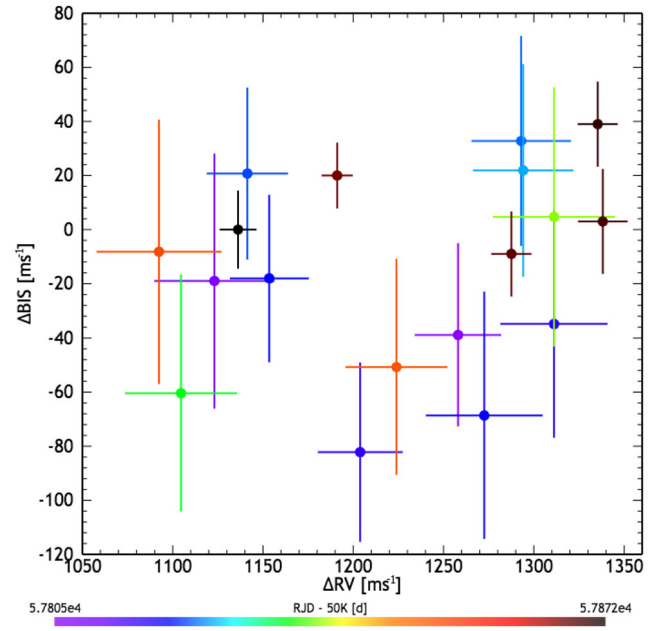


Figure 3. Distribution of the measured radial velocities and associated bisector slopes from CORALIE and HARPS. No evidence of correlation between the two can be seen. Colours represent date of observation between 2017 February 20 and 2017 April 28.

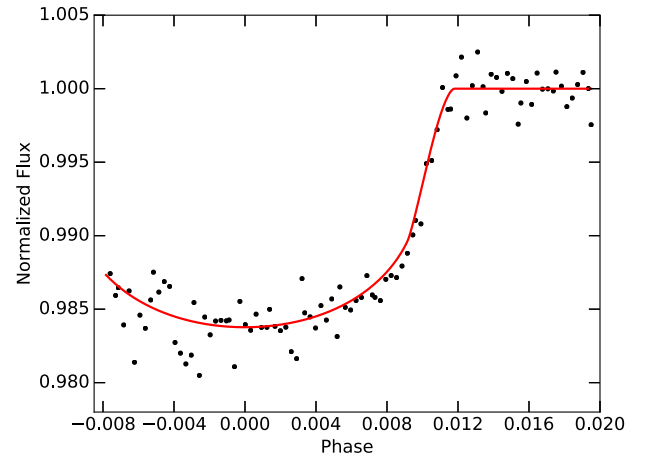


Figure 4. Phase-folded LCO light curve of K2-140 (black points) with best-fitting model plotted as a solid red line (see Section 3.2). Observations occurred the night of 2017 March 18 at the 1-m LCO telescope in Sutherland, South Africa, in ‘i’ band.

The resulting spectrum was used as input of the Zonal Atmospheric Parameter estimator (ZASPE, Brahm et al. 2017b) for computing the stellar atmospheric parameters (T_{eff} , $\log g$, $[\text{Fe}/\text{H}]$ and $v_{\text{rot}} \sin i$) by comparing it with a grid of synthetic spectra generated from the ATLAS9 model atmospheres (Kurucz 1993).

For estimating an initial guess of the physical parameters of the star, we used the Yonsei-Yale Isochrones (Yi et al. 2001) by searching for the M_* and stellar Age of the model that would produce the observed T_{eff} and a/R_* values for the given $[\text{Fe}/\text{H}]$. For obtaining the errors in the physical parameters, we performed Monte Carlo simulations where new values for T_{eff} , a/R_* , and $[\text{Fe}/\text{H}]$ were sampled from Gaussian distributions in each realization.

The resulting physical parameters were used to compute a more precise value for the stellar $\log g$ than the one obtained from

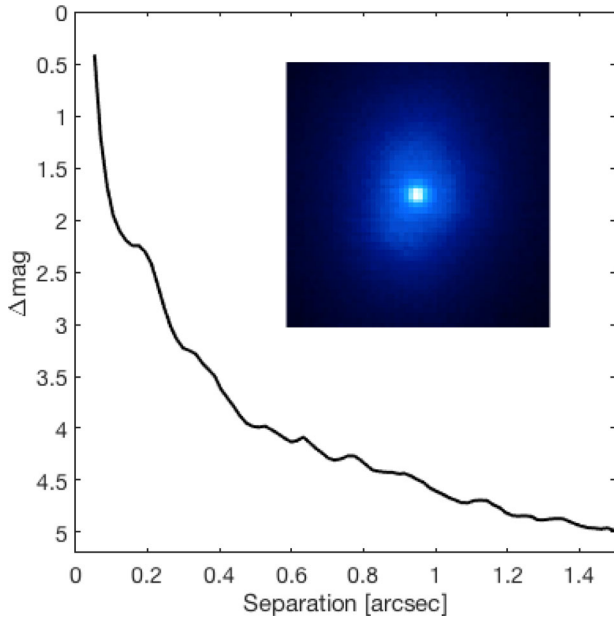


Figure 5. Contrast curve of K2-140 showing the upper limit on the magnitude difference between the target and a possible nearby star as a function of angular separation in arcsec. Data were taken by Robo-AO with the long-pass filter *lp600* covering a wavelength range from 600 nm to close to 1 μ m (Baranec et al. 2014; Jensen-Clem et al. 2017). The inset shows the image of the target spanning 1 arcsec on the side.

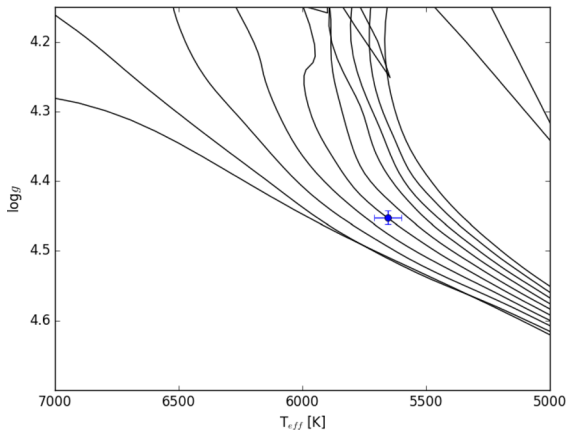


Figure 6. Yonsei-Yale isochrones (Yi et al. 2001) covering (from the left-hand to right-hand side) 0.1, 1, 2, 3, 4, 5, 6, 7, 8, and 9 Gyr based on the stellar parameters determined for K2-140.

spectroscopy. The new $\log g$ value was then held fixed in a new ZASPE execution, whose results are displayed in Table 1. The new atmospheric parameters were used to determine a new set of physical parameters from the Yonsei–Yale Isochrones (Fig. 6), obtaining a stellar mass of $1.005 \pm 0.020 M_{\odot}$, a stellar age of 4.2 ± 1.0 Gyr, and a corresponding stellar radius of $0.987 \pm 0.011 R_{\odot}$, making this host star a slightly metal-rich solar analogue.

Comparing the two results (ISPEC and ZASPE), a very similar effective temperature was measured. However, the ISPEC routine detected a smaller $\log g$ and higher metallicity. We attribute this discrepancy to the HARPS data having a significantly better signal-to-noise ratio than the reconnaissance spectroscopy, which was measured from CORALIE. For further analysis, the results from ZASPE using HARPS data were used.

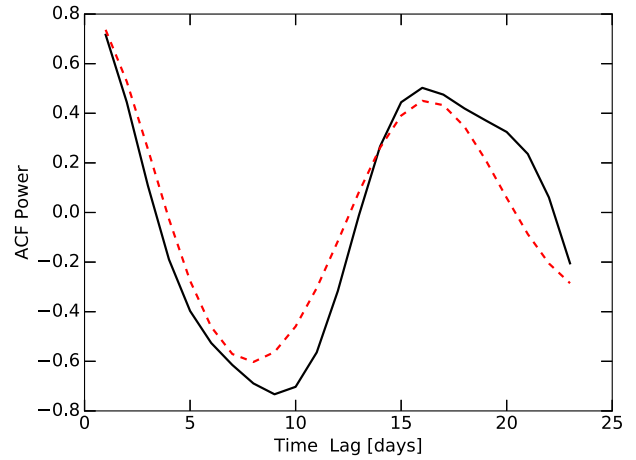


Figure 7. The autocorrelation function (black line) of the light curve for K2-140 with the transits omitted, fitted with a harmonic function (red dashed line) using method described in Giles et al. (2017). This measured a rotation period for K2-140 of 16.3 ± 0.1 d.

We measured the rotation period of K2-140 using an autocorrelation function of the polynomial fit of the K2 light curve (with the transit omitted) as described in Giles et al. (2017). This determined a rotation period of 16.3 ± 0.1 d (Fig. 7). Given $R_* = 0.987^{+0.011}_{-0.011}$, this rotation should result in a $v \sin i \sim 3.1 \text{ km s}^{-1}$, assuming stellar spin axis is perpendicular to the orbital plane of the planet. The spectroscopically derived $v \sin i$ is slightly larger than this value ($v \sin i = 3.8 \pm 0.2$), which may be due to non-equatorial spots and solar-like differential rotation. Such an effect has been seen in other K2 transiting systems, e.g. HATS-36b (Bayliss et al. 2017a).

3.2 Joint fit

We fit the photometry data from Sections 2.1 and 2.3 jointly with the radial velocities from Section 2.2 using the *exonailer*⁵ algorithm (Espinoza et al. 2016). The *exonailer* fitting was conducted with loose priors on the period, P , time of first transit, T_0 , and planet-to-stellar-radii ratio, p (see Table 4 for priors used). These were determined directly from the K2 light curve. In addition, extra (Gaussian) noise terms were added to the errors of the LCO and K2 photometry (in order to empirically estimate extra photometric jitter), with a prior of $\mathcal{N}(1 \text{ 1000})$ for each. Extra Gaussian noise terms were also added to the CORALIE and HARPS radial velocities (in order to model radial-velocity jitter either instrumental or from stellar origin due to, e.g. activity).

Special care was taken in the modelling of the limb-darkening effect, as it is known that this can have a direct impact on the retrieved fitted transit parameters (Espinoza & Jordán 2015). In order to select the best limb-darkening law, we followed Espinoza & Jordán (2016) and ran the *ld-exosim* algorithm,⁶ which gives the mean-square error on each of the retrieved transit parameters for a given limb-darkening law (given the noise, sampling and geometry of the transit). The quadratic law was chosen as it was the law that gave the minimum mean-square error on the planet-to-star radius ratio. For this case, this was the most important transit parameter because it defines the exoplanet’s density. Additionally, the

⁵ <https://github.com/nespinoza/exonailer>

⁶ <https://github.com/nespinoza/ld-exosim>

Table 4. Parameters of K2-140b.

Parameter	Units	Value	Priors ^a
Period	days	$6.569300^{+0.000017}_{-0.000020}$	$\mathcal{N}(6.569, 0.01)$
T_0	days	$2457588.28380^{+0.00014}_{-0.00014}$	$\mathcal{N}(2457588.28544, 0.01)$
T_{14}	hours	4.56 ± 0.29	
T_{23}	hours	3.49 ± 0.26	
$T_{12} = 34$	hours	0.53 ± 0.19	
R_p/R_*		$0.1140^{+0.0015}_{-0.0012}$	$\mathcal{U}(0.05, 0.2)$
b		0.33 ± 0.14	
i	°	$88.51^{+0.69}_{-0.53}$	$\mathcal{U}(80, 90)$
a_*	au	0.0591 ± 0.0034	$\mathcal{U}(3.0, 30.0) [R_*]$
K	km s^{-1}	$0.1112^{+0.0076}_{-0.0073}$	$\mathcal{N}(0.1, 0.1)$
γ_{CORALIE}	km s^{-1}	$1.2170^{+0.0089}_{-0.0092}$	$\mathcal{N}(1.22, 0.05)$
γ_{HARPS}	km s^{-1}	$1.2435^{+0.0068}_{-0.0070}$	$\mathcal{N}(1.24, 0.05)$
CORALIE jitter	km s^{-1}	$0.0041^{+0.0127}_{-0.0037}$	$\mathcal{J}(0.0001, 0.1)$
HARPS jitter	km s^{-1}	$0.0037^{+0.0144}_{-0.0033}$	$\mathcal{J}(0.0001, 0.1)$
Incident flux (F)	$10^8 \text{ erg s}^{-1} \text{ cm}^{-2}$	2.565 ± 0.105	
e		$0.120^{+0.056}_{-0.046}$	$\beta(0.867, 3.03)$
ω	°	$98.88^{+3.85}_{-4.16}$	$\mathcal{U}(0.0, 180.0)$
M_p	M_{Jup}	1.019 ± 0.070	
R_p	R_{Jup}	1.095 ± 0.018	
$\log g_p$	dex (cgs)	3.324 ± 0.033	
ρ_p	ρ_{Jup}	0.726 ± 0.062	
T_{eq}	K	1114 ± 34	

^a $\mathcal{N}(\mu, \sigma)$ is a normal distribution with mean μ and standard deviation σ ; $\mathcal{U}(a, b)$ is a uniform distribution between values a and b ; $\mathcal{J}(a, b)$ is a Jeffrey's distribution with a lower limit of a and b ; and $\beta(a, b)$ is a Beta distribution with parameters a and b as described by Kipping (2013a).

limb-darkening coefficients were individually fitted for the K2 and LCO light curves, as they have different response functions and span different wavelength ranges. An initial fit assuming different planet-to-star radius ratios for each data set was also made, but both independently gave consistent parameters with no wavelength dependence. The final fit was made by using a common planet-to-star radius ratio for both data sets. Priors for the limb-darkening coefficients were set to be $\mathcal{N}(0, 1)$, an uninformative transformation of the quadratic limb-darkening parameters (see Kipping 2013b).

We tried fits assuming circular and non-circular orbits and the results favour the non-circular orbit, which gave an eccentricity of $0.120^{+0.056}_{-0.046}$ and an argument of periapsis of $98.88^{+3.85}_{-4.16}$ °.

The final fits for the K2 and LCO light curves are shown in red in Figs 1 and 4, and for the radial-velocities in Fig. 2. The priors and posterior values of the fitted parameters with *exonailer* are listed in Table 4. As can be seen, the photometric jitter is significant only for the K2 light curve; the LCO photometric jitter is consistent with zero. This is due to the fact that we decided to estimate the errors directly from the K2 photometry, whereas the extra jitter was added in quadrature to the LCO errorbars given by the photometric pipeline. For the radial-velocity jitter, it can be seen that the extra term for both instruments is also consistent with zero.

3.3 Planet parameters

exonailer was able to determine various system parameters from the light curve transit shape: a/R_* , the semi-major axis-to-stellar radius ratio; R_p/R_* , the ratio of planetary to stellar radius (given as p in *exonailer*); t_0 , the time of the first observed transit; P , the orbital period of the planet; and i , the inclination of the planet's orbit. Additionally, from the radial velocity curves: e , the

eccentricity; ω , the periapsis argument; and K , the radial velocity semi-amplitude of the star. Through a combination of these parameters and the already determined stellar mass and radius from Section 3.1, further properties of the planet can be determined using the equations as described in Seager & Mallén-Ornelas (2003). We measured the planetary mass to be $1.019 \pm 0.070 M_{\text{Jup}}$ with a radius of $1.095 \pm 0.018 R_{\text{Jup}}$. This indicates a bulk density which is slightly less than that of Jupiter, $0.726 \pm 0.062 \rho_{\text{Jup}}$. The planet has an incident flux of $2.565 \pm 0.105 \times 10^8 \text{ erg s}^{-1} \text{ cm}^{-2}$. The predicted equilibrium temperature is $1114 \pm 34 \text{ K}$, with the assumption of a blackbody and an efficient transfer of energy from the day- to night-side. These are all listed in Table 4.

4 DISCUSSION

In this section, we compare the properties of K2-140b to the population of known hot Jupiters, and for this purpose, we use the NASA Exoplanet Archive⁷ (Akeson et al. 2013) as accessed on 2017 June 6.

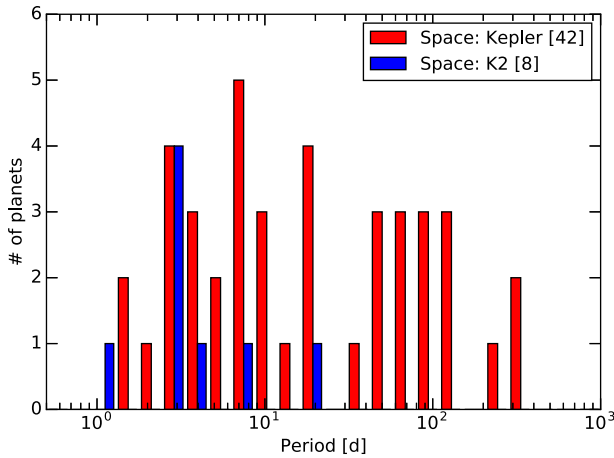
4.1 Orbital period

For warm and hot Jupiters, *Kepler* dominates the number of discoveries for planets with orbital periods equivalent to or longer than that of K2-140b. Therefore, to investigate the ability of K2 to find longer period warm and hot Jupiters, we compare the *Kepler* and K2 discoveries within a subset of all confirmed planets. They all have masses greater than $0.2 M_{\text{Jup}}$ and have other significant parameters – such as eccentricity, planet density, and planet

⁷ exoplanetarchive.ipac.caltech.edu

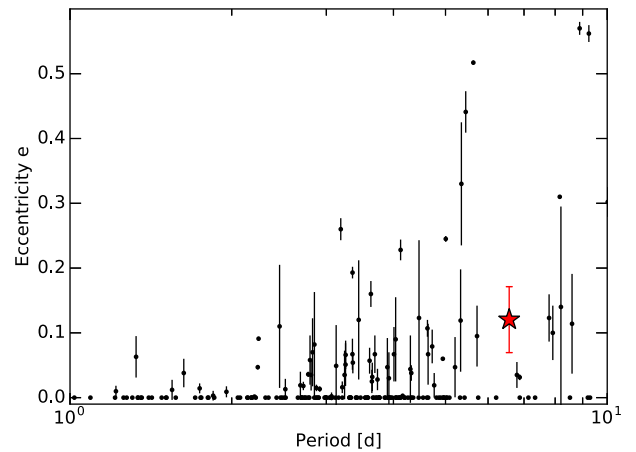
Table 5. *K2* discovered warm and hot Jupiters with precise measurements (20 per cent) on the masses and radii.

Planet	P_{orb} (d)	Mass (M_{Jup})	Radius (R_{Jup})	Reference
K2-29b	3.2588321 ± 0.0000019	0.73 ± 0.04	1.19 ± 0.02	Santerne et al. (2016)
"	3.2589263 ± 0.0000015	$0.613^{+0.027}_{-0.026}$	$1.000^{+0.071}_{-0.067}$	Johnson et al. (2016)
K2-30b	4.098503 ± 0.000011	$0.579^{+0.028}_{-0.027}$	$1.039^{+0.050}_{-0.051}$	Johnson et al. (2016)
"	4.098513 ± 0.000018	0.625 ± 0.030	1.197 ± 0.052	Lillo-Box et al. (2016)
"	$4.09849^{+0.00002}_{-0.00002}$	$0.589^{+0.023}_{-0.022}$	$1.069^{+0.023}_{-0.019}$	Brahm et al. (2016a)
K2-31b	1.257850 ± 0.000002	1.774 ± 0.079	$0.71 - 1.41$	Grziwa et al. (2016)
K2-34b	$2.9956675^{+0.0000075}_{-0.0000071}$	1.649 ± 0.098	1.217 ± 0.053	Lillo-Box et al. (2016)
"	2.995654 ± 0.000018	1.773 ± 0.086	1.44 ± 0.16	Hirano et al. (2016)
"	$2.995629^{+0.000006}_{-0.000006}$	$1.698^{+0.061}_{-0.050}$	$1.377^{+0.14}_{-0.13}$	Brahm et al. (2016a)
K2-60b	3.00265 ± 0.00004	0.426 ± 0.037	0.683 ± 0.037	Eigmüller et al. (2017)
K2-97b	8.4016 ± 0.0015	1.10 ± 0.11	1.31 ± 0.11	Grunblatt et al. (2016)
K2-99b	18.249 ± 0.001	0.97 ± 0.09	1.29 ± 0.05	Smith et al. (2017)
K2-107b	3.31392 ± 0.00002	0.84 ± 0.08	1.44 ± 0.15	Eigmüller et al. (2017)

**Figure 8.** Distribution of confirmed planets found with *Kepler* and *K2* with masses $> 0.2M_{\text{Jup}}$. *Kepler* is in red and *K2* is in blue. K2-140b has been included into the *K2* distribution.

radius – also measured. Currently, *K2* has only discovered eight planets within this subset where K2-140b is the third longest orbital period (see Table 5).

The number of planets discovered by *Kepler* and *K2* over the period range strongly reveals that, as expected, *K2* is less sensitive to long-period planets than *Kepler*, equally sensitive to short-period planets (Fig. 8). *Kepler* observed 156 000 stars and, to date, *K2* has observed a total of 171 610 (all stars observed by *K2* in long cadence from Campaigns 1–10). However, there will be a natural ramping down of the detection efficiency for planets with periods of ~ 30 – 40 d for *K2* as campaigns typically do not last longer than 80 d – whereas, for *Kepler*, there was almost 4 yr of continuous observation of the survey. Additionally, due to the necessary follow-up time required per planet (radial velocity, imaging etc.), the community has had much longer to confirm *Kepler* candidates compared with *K2* candidates – there are still regular announcements of discoveries from older *K2* campaigns as well as discoveries from the current campaign. Given more time, the distribution for planets with orbital periods of 40 d or less in *K2* may reach a similar distribution to *Kepler*. By the conclusion of the *K2* mission (assuming 19 full

**Figure 9.** Eccentricities of transiting hot Jupiters ($P = 1$ – 10 d, $M_P > 0.2M_{\text{Jup}}$). K2-140b is plotted as a red star. Planets with undetermined eccentricities have been excluded.

campaigns), we may expect *K2* will produce more than double the number of transiting giant planets with periods < 10 d compared to *Kepler*.

Within the ranges of warm and hot Jupiters, ground-based surveys, in fact, dominate for shorter orbital periods. There are only 11 ground-based discoveries (NASA Exoplanet Archive, Akesson et al. 2013) with periods longer than that of K2-140b. This shows that, compared to ground-based surveys, *K2* is more effective at detecting longer period warm and hot Jupiters.

4.2 Eccentricity

Exoplanets that have non-zero eccentricities are bodies that have typically either been excited out of their orbits by other bodies or are migrating to a new orbit. The eccentric orbit of K2-140b has the potential to increase our understanding of these mechanisms.

In Fig. 9, we plot the measured eccentricities for transiting hot Jupiters with periods between 1 and 10 d. This was a subset of all confirmed planets with masses greater than $0.2M_{\text{Jup}}$ (and as previously, has other significant parameters measured). Below

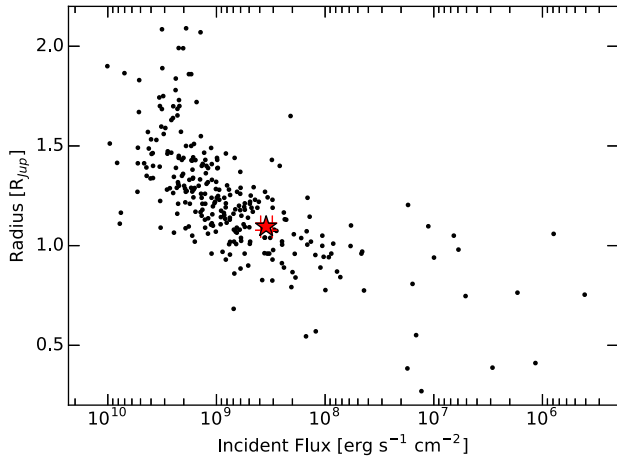


Figure 10. Distribution of incident flux and planet radii of confirmed planets found with measured masses (masses greater than $0.2M_{\text{Jup}}$) and other measured properties. This work is represented by the red star and all other warm, hot Jupiters by black points.

~ 5.5 d, approximately 70 percent of hot Jupiters have measured eccentricity consistent with 0. However for systems with period greater than 5.5, this fraction drops below 50 percent. It is therefore not surprising that we find a non-zero eccentricity for K2-140b ($e = 0.120^{+0.056}_{-0.046}$). If we assume a Q-factor of 10^6 (Wu 2005), we calculate (Goldreich & Soter 1966) a tidal circularization time-scale of $\tau_e = 2.577$ Gyr. Given our best estimate for the age of the system (4.22 ± 0.95 Gyr), this means that the time-scale is of the same order of the age of the star.

4.3 Planet atmosphere inflation

A common avenue of investigation associated with warm and hot Jupiters is determining whether they are inflated or not. The distribution of the incident flux on a planet and its radii for warm and hot Jupiters is from a subset of confirmed planets with masses greater than $0.2M_{\text{Jup}}$ and with other significant parameters measured. Based on the mass and radius of K2-140b, it is slightly inflated compared with Jupiter, but not inflated with respect to other exoplanets with similar incident flux (see Fig. 10). The planet receives an incident flux of $2.565 \pm 0.105 \times 10^8 \text{ erg s}^{-1} \text{ cm}^{-2}$, which is very close to the empirical limit for inflation ($2 \times 10^8 \text{ erg s}^{-1} \text{ cm}^{-2}$ Demory & Seager 2011). Discovering exoplanet in this incident flux regime is important for studying the onset of the mechanism by which hot Jupiters are inflated.

5 CONCLUSIONS

We found a hot-Jupiter planet in data from K2 Campaign 10 and followed it up with radial velocity measurements and high angular resolution imaging. K2-140b orbits a $V = 12.624 \pm 0.030$, 4.22 ± 0.95 Gyr star with a $[\text{Fe}/\text{H}]$ of 0.12 ± 0.045 . The planet has a non-circular orbit with an eccentricity of $0.120^{+0.056}_{-0.046}$ and period of 6.57 d and a mass and radius of $1.019 \pm 0.070M_{\text{Jup}}$ and $1.095 \pm 0.018R_{\text{Jup}}$, respectively. It is the third longest period giant exoplanet discovered from K2 and has a period longer period than 94 percent of giant planets discovered from ground-based transit surveys.

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SUPPORTING INFORMATION

Supplementary data are available at *MNRAS* online.

Table 2. Photometry for EPIC 228735255.

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